

### Changing Dimensions for Area & Volume

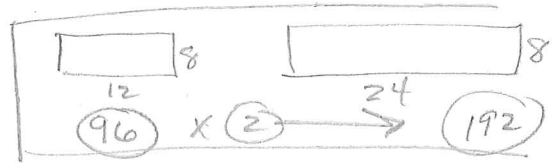
1. Draw a rectangle with a length of 12 cm and a width of 8 cm. Find the area. 96 cm<sup>2</sup>



$$A = bh$$

$$= 8 \cdot 12$$

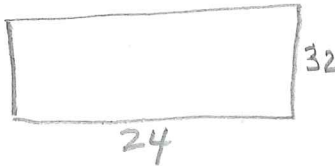
$$= 96 \text{ cm}^2$$



Apply a scale factor of 2 to the length and 4 to the width. Draw the new rectangle and find the area. 768 cm<sup>2</sup>

$$L = 12 \cdot 2 = 24$$

$$W = 8 \cdot 4 = 32$$



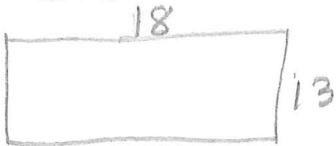
$$A = bh$$

$$= 24 \cdot 32$$

$$= 768 \text{ cm}^2$$

The new rectangle has an area that is 8 times greater than the area of the original rectangle.

2. Draw a rectangle with a length of 18 in and a width of 13 in. Find the area. 234 in<sup>2</sup>



$$A = bh$$

$$= 13 \cdot 18$$

$$A = 234 \text{ in}^2$$

Apply a scale factor of 5 to the length and 3 to the width. Draw the new rectangle and find the area. 3510 in<sup>2</sup>



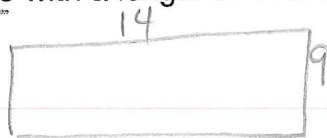
$$A = bh$$

$$= 90 \cdot 39$$

$$A = 3510 \text{ in}^2$$

The new rectangle has an area that is 15 times greater than the area of the original rectangle.

3. Draw a rectangle with a length of 14 ft and a width of 9 ft. Find the area. 126 ft<sup>2</sup>

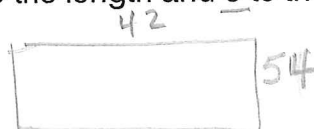


$$A = bh$$

$$= 14 \cdot 9$$

$$A = 126 \text{ ft}^2$$

Apply a scale factor of 3 to the length and 6 to the width. Draw the new rectangle and find the area. 2268 ft<sup>2</sup>



$$A = bh$$

$$= 42 \cdot 54$$

$$A = 2268 \text{ ft}^2$$

The new rectangle has an area that is 18 times greater than the area of the original rectangle.

Describe the relationship that you see:

Answers will vary: (Possible answer)

A learned that multiplying the 2 scale factors together will give me the scale factor that was applied to the new figure.

4. Draw a rectangular prism with a length of 6 cm, a width of 3 cm, and a height of 2 cm. Find the volume.  $36 \text{ cm}^3$



$$\begin{aligned} \text{Vol} &= Bh \\ &= 18 \cdot 2 \end{aligned}$$

$$\text{Vol} = 36$$

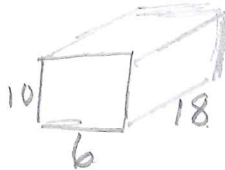
$$A = bh$$

$$= 3 \cdot 6$$

$$A = 18 \text{ cm}^2$$

Area of the Base (B)

Apply a scale factor of 3 to the length, 2 to the width, and 5 to the height. Draw the new rectangular prism and find the volume.  $1080 \text{ cm}^3$



$$\begin{aligned} \text{Vol} &= Bh \\ &= 108 \cdot 10 \end{aligned}$$

$$\text{Vol} = 1080$$

$$A = bh$$

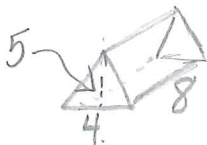
$$= 6 \cdot 18$$

$$= 108 \text{ cm}^2$$

Area of the Base (B)

The new rectangular prism has a volume that is 30 times greater than the volume of the original rectangular prism.

5. Draw a triangular prism with a base of 4 ft, a height of 5 ft, and a depth of 8 ft. Find the volume.  $80 \text{ ft}^3$



$$\begin{aligned} \text{Vol} &= Bh \\ &= 10 \cdot 8 \end{aligned}$$

$$\text{Vol} = 80 \text{ ft}^3$$

Area of  $\Delta$

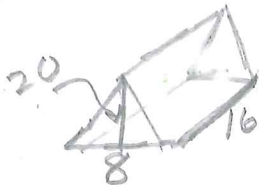
$$A = \frac{1}{2}bh$$

$$= \frac{1}{2}4 \cdot 5$$

$$A = 10 \text{ ft}^2$$

Area of the Base (B)

Apply a scale factor of 2 to base, 4 to the height, and 2 to the depth. Draw the new triangular prism and find the volume.  $1280 \text{ ft}^3$



$$\text{Vol} = Bh$$

$$= 80 \cdot 16$$

$$\text{Vol} = 1280 \text{ ft}^3$$

$$A = \frac{1}{2}bh$$

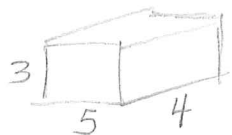
$$= \frac{1}{2}8 \cdot 20$$

$$A = 80 \text{ ft}^2$$

Area of the Base (B)

The new triangular prism has a volume that is 16 times greater than the volume of the original triangular prism.

6. Draw a **rectangular prism** with a length of 4 in, a width of 5 in, and a height of 3 in. Find the **volume**. 60 in<sup>3</sup>



$$\begin{aligned} \text{Vol} &= Bh \\ &= 20 \cdot 3 \\ \text{Vol} &= 60 \text{ in}^3 \end{aligned}$$

$$\begin{aligned} A &= bh \\ &= 5 \cdot 4 \\ A &= 20 \text{ in}^2 \\ &\text{Area of the Base (B)} \end{aligned}$$

Apply a **scale factor** of 2 to the length, 4 to the width and 10 to the height. Draw the **new rectangular prism** and find the **volume**. 4800 in<sup>3</sup>



$$\begin{aligned} \text{Vol} &= Bh \\ &= 160 \cdot 30 \\ \text{Vol} &= 4800 \text{ in}^3 \end{aligned}$$

$$\begin{aligned} A &= bh \\ &= 20 \cdot 8 \\ A &= 160 \text{ in}^2 \\ &\text{Area of the Base (B)} \end{aligned}$$

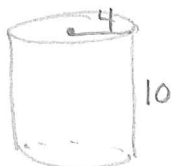
The **new rectangular prism** has a volume that is 80 times greater than the volume of the **original rectangular prism**.

Describe the relationship that you see: Answers will vary

Possible answer:

I noticed that if I multiplied each scale factor that was applied to the original shape together it was equal to how many times greater the new shape was to the original shape.

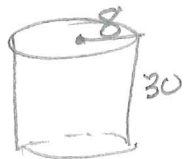
7. Draw a **cylinder** with a radius of 4 in and a height of 10 in. Find the **volume**. 502.4 in<sup>3</sup>



$$\begin{aligned} \text{Vol} &= Bh \\ &= 50.24 \cdot 10 \\ \text{Vol} &= 502.4 \text{ in}^3 \end{aligned}$$

$$\begin{aligned} A &= \pi r^2 \\ &= 3.14 \cdot 4^2 \\ &= 3.14 \cdot 16 \\ A &= 50.24 \end{aligned}$$

Apply a **scale factor** of 2 to the radius and 3 to the height. Draw the new cylinder and find the **volume**. 6028.8 in<sup>3</sup>



$$\begin{aligned} \text{Vol} &= Bh \\ &= 200.96(30) \\ \text{Vol} &= 6028.8 \text{ in}^3 \end{aligned}$$

$$\begin{aligned} A &= \pi r^2 \\ &= 3.14 \cdot 8^2 \\ &= 3.14 \cdot 64 \\ A &= 200.96 \end{aligned}$$

The **new cylinder** has a volume that is 12 times greater than the volume of the **original cylinder**.

I noticed that the area of the base of the original cylinder was 50.24 in<sup>2</sup>. The area of the base of the new cylinder was 200.96 in<sup>2</sup> which means the new area is 4 times the original base. Then 4 times the scale factor of 3 applied to the height is 12.

$$\begin{array}{r} 6028.8 \div 502.4 = 12 \\ \text{Vol. orig.} \quad \text{Vol. new} \end{array}$$

8. Draw a cylinder with a radius of 3 ft and a height of 8 ft. Find the volume. 226.08 ft<sup>3</sup>



$$\text{Vol} = Bh$$

$$= 28.26 \cdot 8$$

$$A = \pi r^2$$

$$= 3.14 \cdot 3^2$$

$$\text{Vol} = 226.08 \text{ ft}^3 \quad A = 28.26$$

Apply a scale factor of 3 to the radius and 5 to the height. Draw the new cylinder and find the volume. 10,173.6 ft<sup>3</sup>



$$\text{Vol} = Bh$$

$$= 254.34 \cdot 40$$

$$A = \pi r^2$$

$$= 3.14 \cdot 9^2$$

$$\text{Vol} = 10,173.6 \text{ ft}^3 \quad A = 254.34$$

The new cylinder has a volume that is 45 times greater than the volume of the original cylinder.

$$10,173.6 \div 226.08 = 45$$

$$\text{radius} = 3 \times \text{scale factor of } 3 = 9 \times \text{height of } 5 = 45$$

9. Draw a cylinder with a radius of 6 cm and a height of 5 cm. Find the volume. 565.2 cm<sup>3</sup>



$$\text{Vol} = Bh$$

$$= (113.04) 5$$

$$\text{Area} = \pi r^2$$

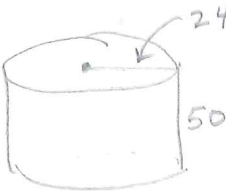
$$= 3.14 \cdot 6^2$$

$$\text{Vol} = 565.2 \text{ cm}^3$$

$$= 3.14 \cdot 36$$

$$A = 113.04 \text{ cm}^2$$

Apply a scale factor of 4 to the radius and 10 to the height. Draw the new cylinder and find the volume. 90432 cm<sup>3</sup>



$$\text{Vol} = Bh$$

$$= (808.64) 50$$

$$\text{Area} = \pi r^2$$

$$= (3.14) 24^2$$

$$\text{Vol} = 90432 \text{ cm}^3$$

$$= (3.14) 576$$

$$A = 1808.64 \text{ cm}^2$$

The new cylinder has a volume that is 160 times greater than the volume of the original cylinder.

$$90432 \div 565.2 = 160$$

$$r = 4 \times \text{scale factor of } 4 = 16 \times \text{scale factor of } 10 \text{ to height} = 160$$

Describe the relationship that you see:

Answers will vary:

Since the radius is squared for B, then you square the scale factor applied to the radius ( $4^2 = 16$ ) then multiply that by the scale factor applied to the height which is 10, therefore  $16 \times 10 = \underline{\underline{160}}$ .

Since the radius is squared for B, then you square the scale factor applied to the radius ( $3^2 = 9$ ) then multiply that by the scale factor applied to the height which is 5, therefore  $9 \times 5 = \underline{\underline{45}}$ !